

Decoding for SMT

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About this talk

This talk is not

- ▶ a review of beam search, cube pruning or any specific decoding algorithm

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This talk is about

- ▶ understanding what makes decoding difficult

For starters

Let's think of decoding as referring to an inference task

- ▶ making predictions
 - ▶ decisions in a highly combinatorial space of possibilities

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(discuss tractability issues)

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 - ▶ decisions in a highly combinatorial space of possibilities

Goals

1. characterise the space of solutions
(discuss tractability issues)
2. understand the impact of parameterisation
3. survey decoding techniques

Task

Translate a source text (e.g. sentence)

Examples:

<i>um conto de duas cidades</i>	→	a tale of two cities
<i>nosso amigo comum</i>	→	our mutual friend
<i>a loja de antiguidades</i>	→	the old curiosity shop
<i>o grill da lareira</i>	→	the cricket on the hearth

Model of translational equivalences

Defines the space of possible translations

- ▶ think of it as a recipe to generate translations
[Lopez, 2008]

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Example:

- ▶ a word replacement model
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- ▶ with no insertions or deletions
- ▶ constrained to known word-to-word bilingual mappings
(rule set)

Monotone word-by-word translation: solutions

Source: *um conto de duas cidades*

Translation rules¹

um {a, some, one}

conto {tale, story, narrative, novella}

de {of, from, 's}

duas {two, couple}

cidades {cities, towns, villages}

¹Unrealistically simple

Monotone word-by-word translation: solutions

<i>um</i>	{a, some, one}
<i>conto</i>	{tale, story, narrative, novella}
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um conto de duas cidades

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um conto de duas cidades
a tale of two cities

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a tale of two **towns**

Monotone word-by-word translation: solutions

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a tale of two cities

a tale of two **towns**

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um conto de duas cidades

a tale of two cities

a tale of two **towns**

a tale of two **villages**

a tale of **couple cities**

Monotone word-by-word translation: solutions

um conto de duas cidades

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a tale of two **towns**

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Monotone word-by-word translation: solutions

um conto de duas cidades

a tale of two cities

a tale of two **towns**

a tale of two **villages**

a tale of **couple cities**

a tale of couple **towns**

...

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This can go very far :(

Monotone word-by-word translation: complexity

Say

- ▶ the input has I words
- ▶ we know at most t translation options per source word

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This makes $O(t^I)$ solutions

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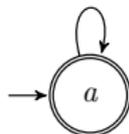
Note

- ▶ WMT14's shared task: $I = 40$ on average
- ▶ last I checked Moses default was $t = 100$
(for a more complex model)
- ▶ silly monotone word replacement model: 10^{80} solutions

Space of solutions as intersection/composition



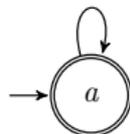
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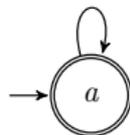
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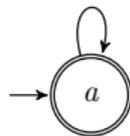
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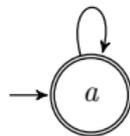
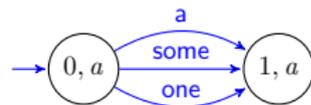
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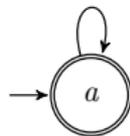
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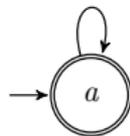
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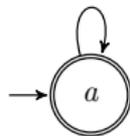
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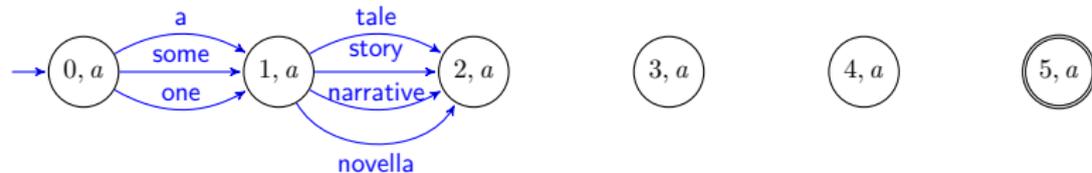
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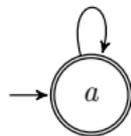
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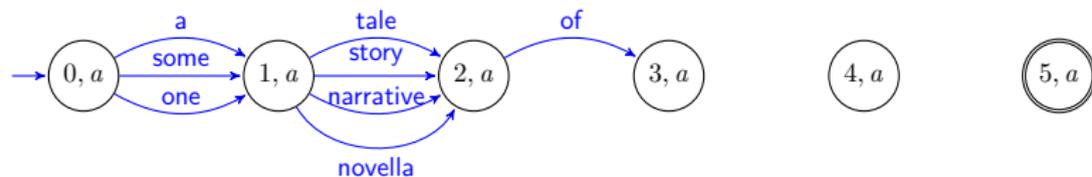
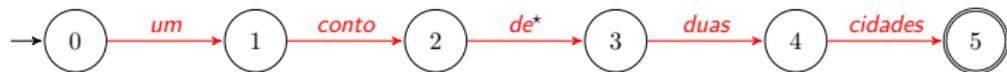
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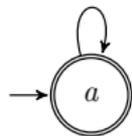
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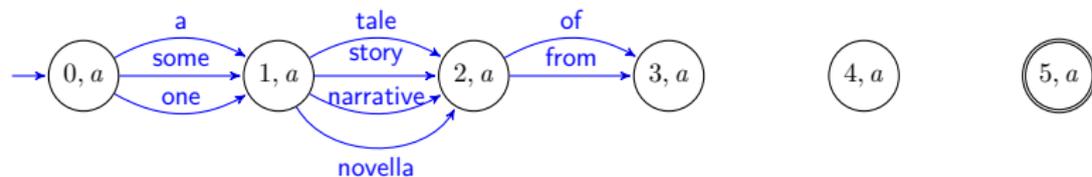
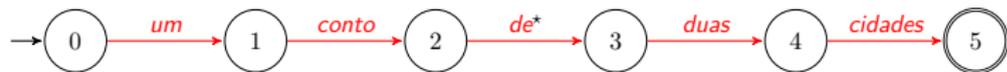
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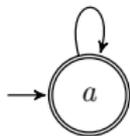
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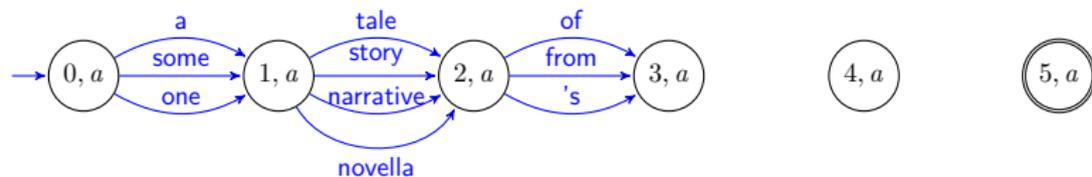
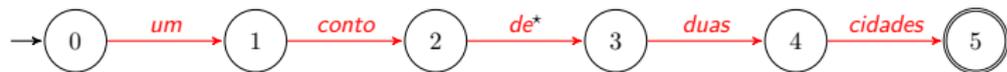
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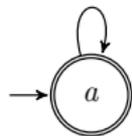
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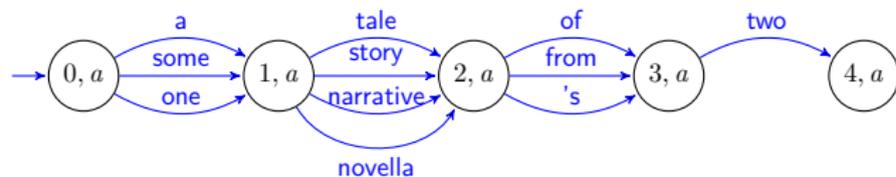
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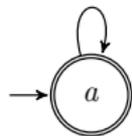
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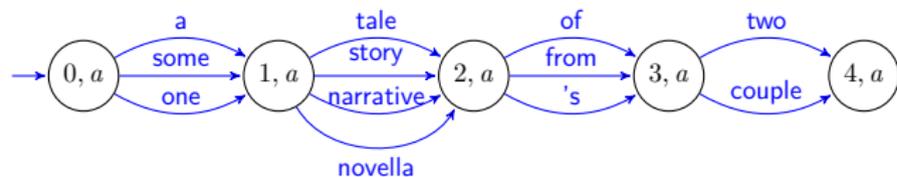
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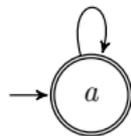
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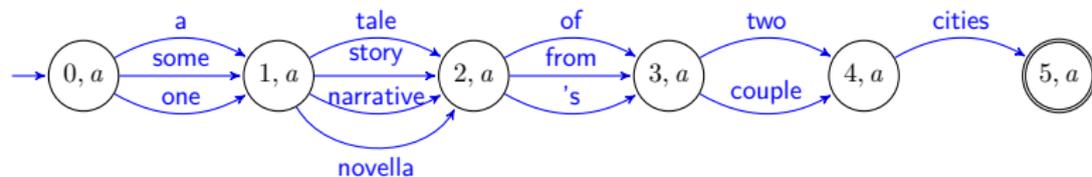
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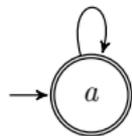
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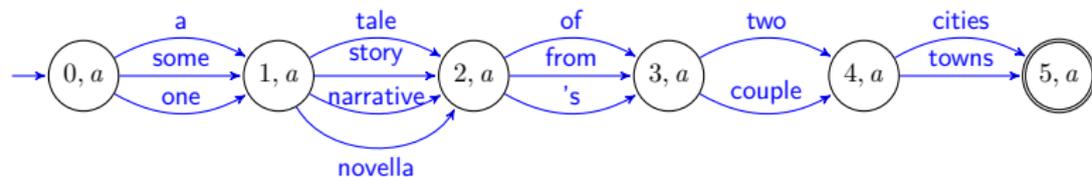
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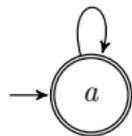
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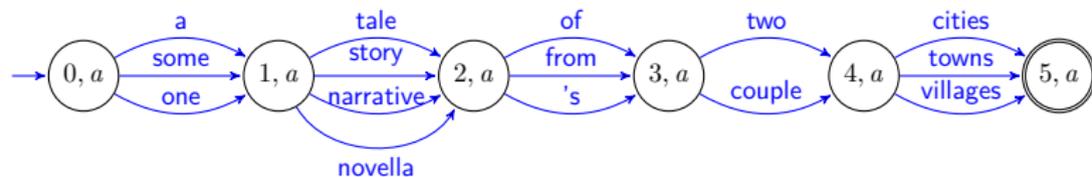
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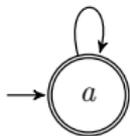
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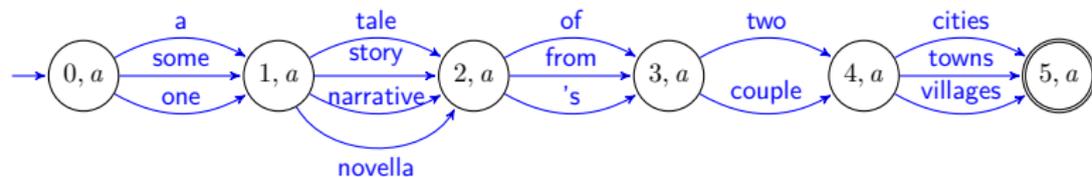
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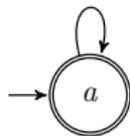
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$3 \times 4 \times 3 \times 2 \times 3 = 216$ solutions

▶ 6 states

▶ $3 + 4 + 3 + 2 + 3 = 15$ transitions

Packing solutions with finite-state automata

Same $O(t^I)$ solutions using

- ▶ $O(I)$ states
- ▶ $O(tI)$ transitions

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- ▶ exponential number of solutions in linear space

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- ▶ exponential number of solutions in linear space
- ▶ translates infinitely many sentences

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- ▶ set of translations given by composition
- ▶ exponential number of solutions in linear space
- ▶ translates infinitely many sentences

but not nearly enough interesting cases!

Monotone word-by-word translation: fail!

nosso {our, ours}
amigo {friend, mate}
comum {ordinary, common, usual, mutual}



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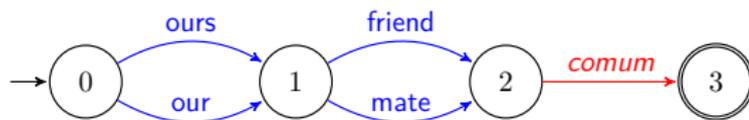


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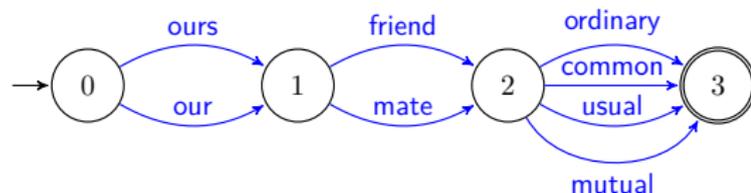


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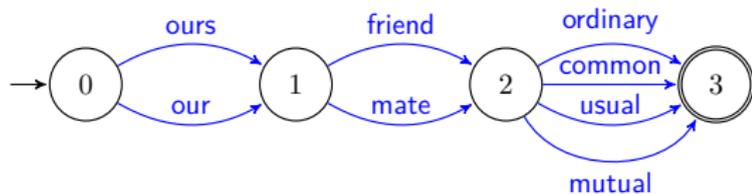
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We simply cannot obtain a correct translation

our mutual friend

Reordering

Our model of translational equivalences assumes monotonicity

- ▶ a word replacement model
- ▶ operates in **monotone** left-to-right order
- ▶ with no insertions or deletions
- ▶ constrained to known word-to-word bilingual mappings (rule set)

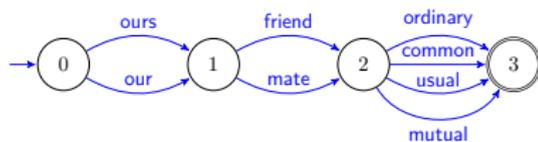
Reordering

Not anymore!

- ▶ a word replacement model
- ▶ operates in **arbitrary** order
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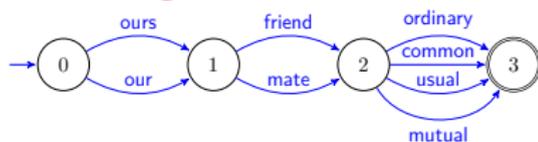
Translating arbitrary permutations

nosso amigo comum

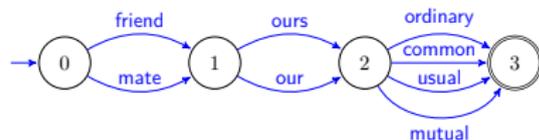


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nosso amigo comum

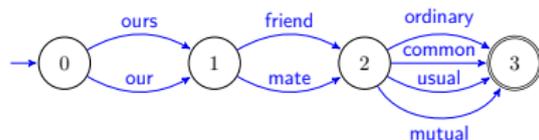


amigo nosso comum

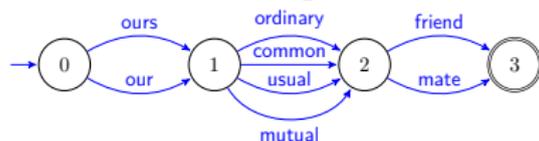


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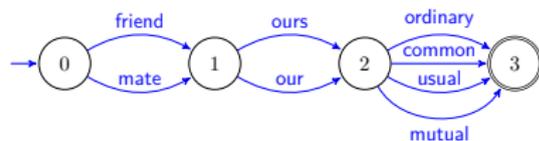
nosso amigo comum



nosso comum amigo

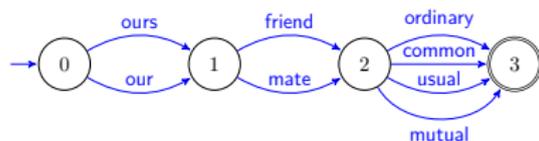


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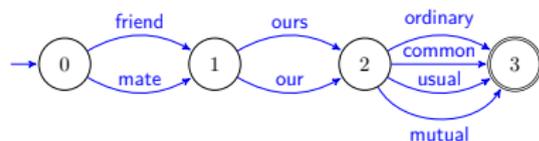


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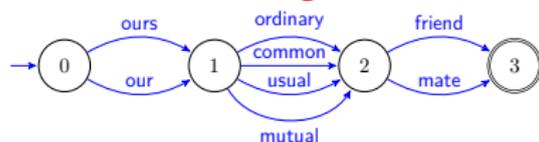
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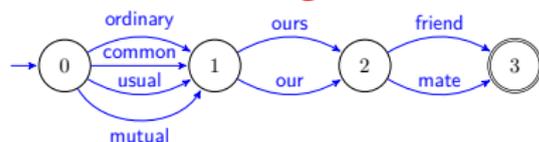
amigo nosso comum



nosso comum amigo

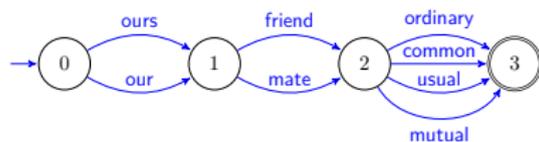


comum nosso amigo

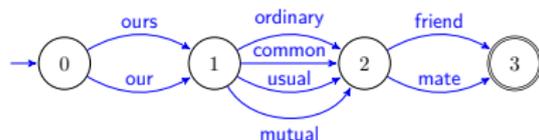


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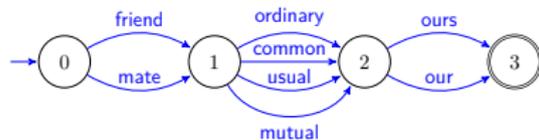
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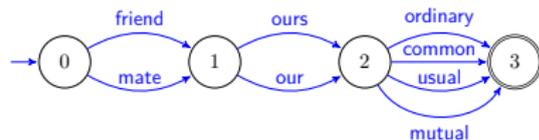
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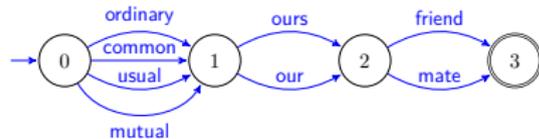
amigo comum nosso



amigo nosso comum

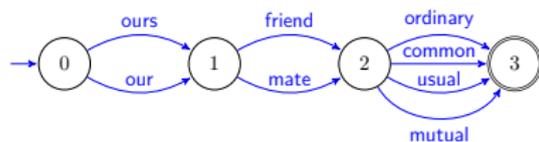


comum nosso amigo

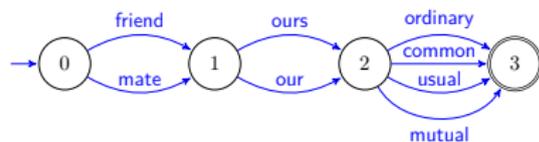


Translating arbitrary permutations

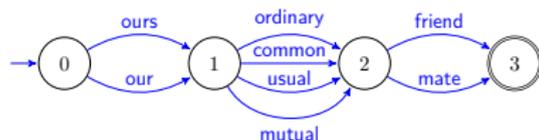
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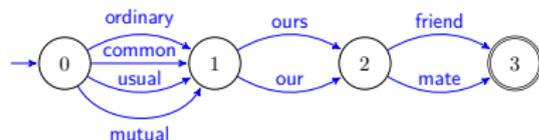
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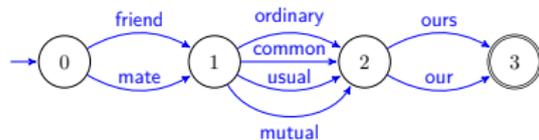
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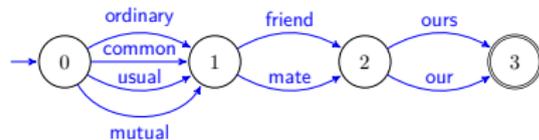
comum nosso amigo



amigo comum nosso

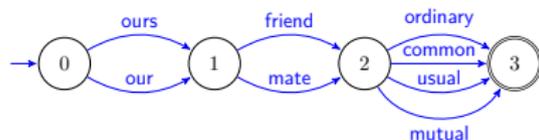


comum amigo nosso

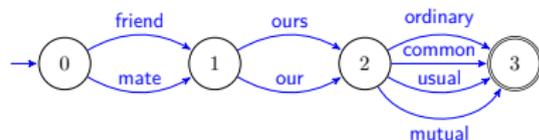


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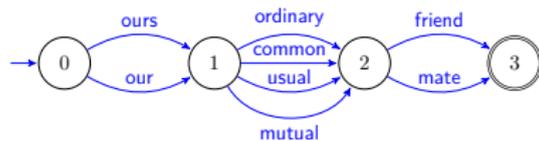
nosso amigo comum



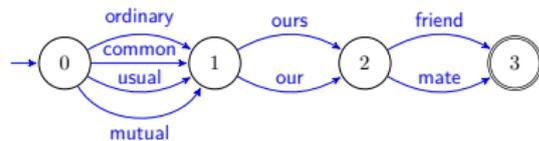
amigo nosso comum



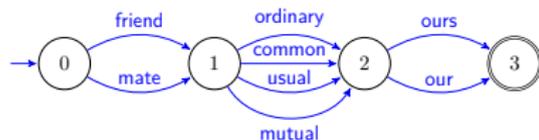
nosso comum amigo



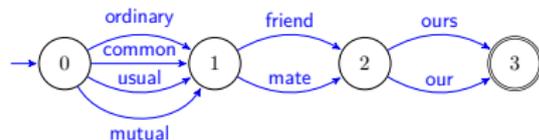
comum nosso amigo



amigo comum nosso



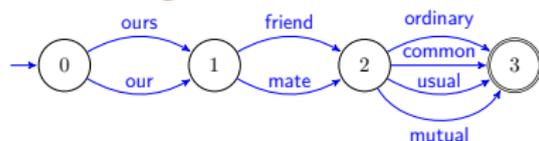
comum amigo nosso



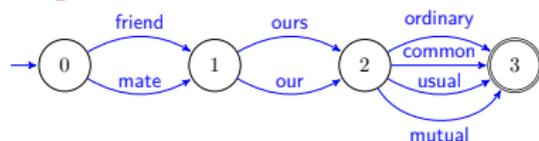
$3! = 3 \times 2 \times 1 = 6$ permutations

Translating arbitrary permutations

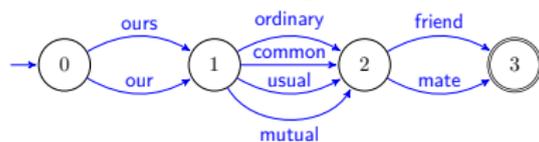
nosso amigo comum



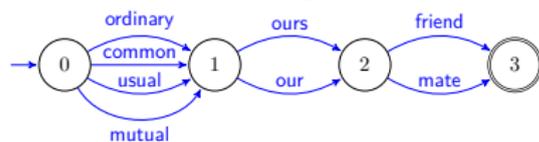
amigo nosso comum



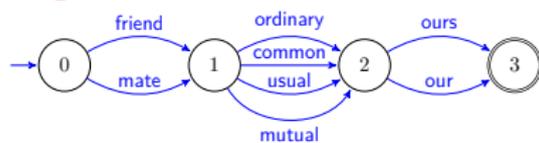
nosso comum amigo



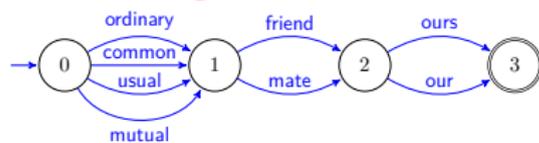
comum nosso amigo



amigo comum nosso



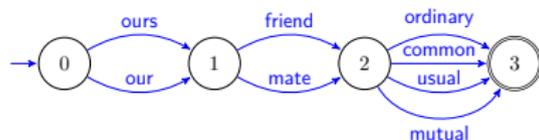
comum amigo nosso



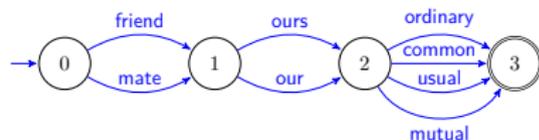
each has $2 \times 2 \times 4 = 16$ translations

Translating arbitrary permutations

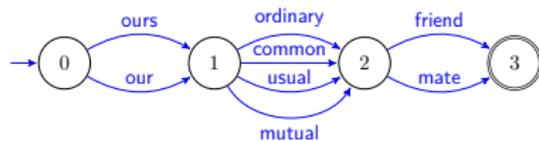
nosso amigo comum



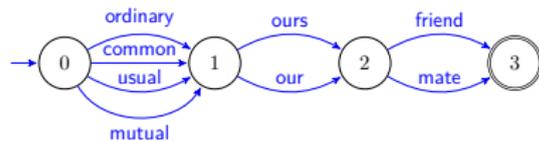
amigo nosso comum



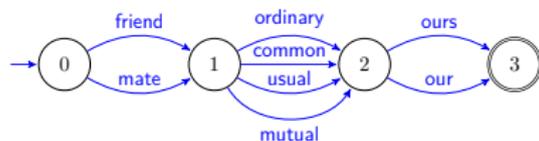
nosso comum amigo



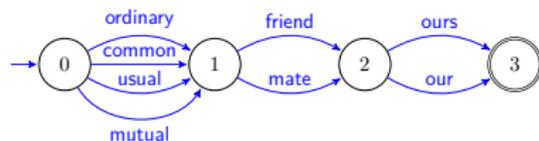
comum nosso amigo



amigo comum nosso



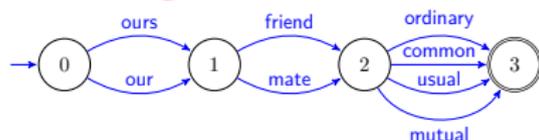
comum amigo nosso



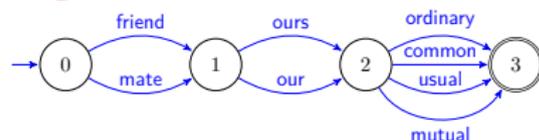
amounting to $6 \times 16 = 96$ solutions

Translating arbitrary permutations

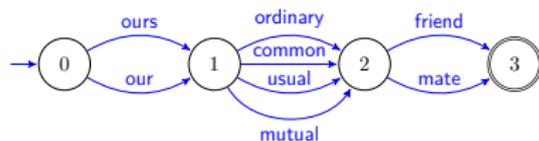
nosso amigo comum



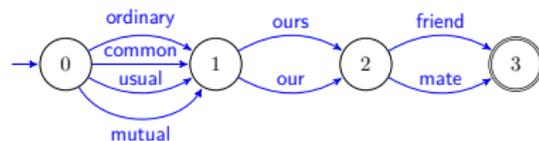
amigo nosso comum



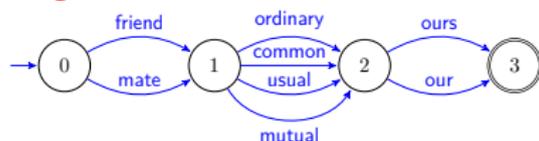
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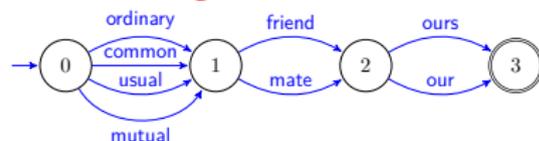
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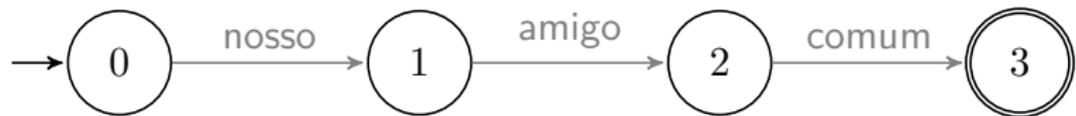


comum amigo nosso



$I!$ permutations $\times t^I$ translations

Packing permutations



Packing permutations



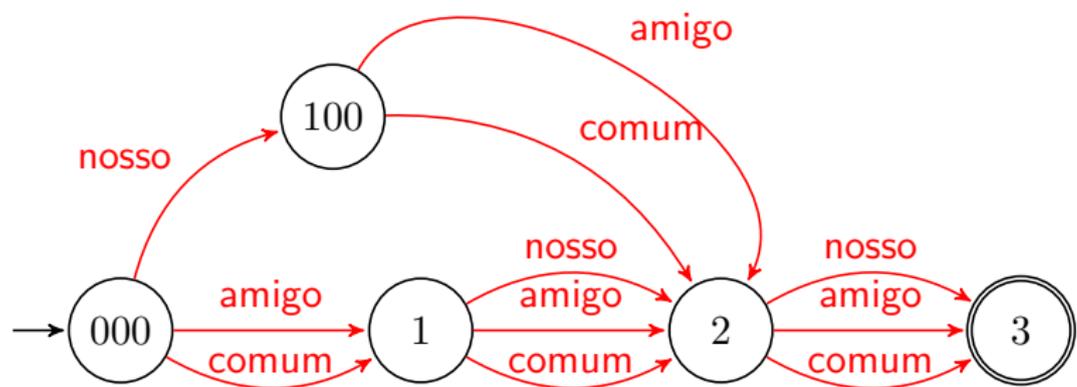
Packing permutations



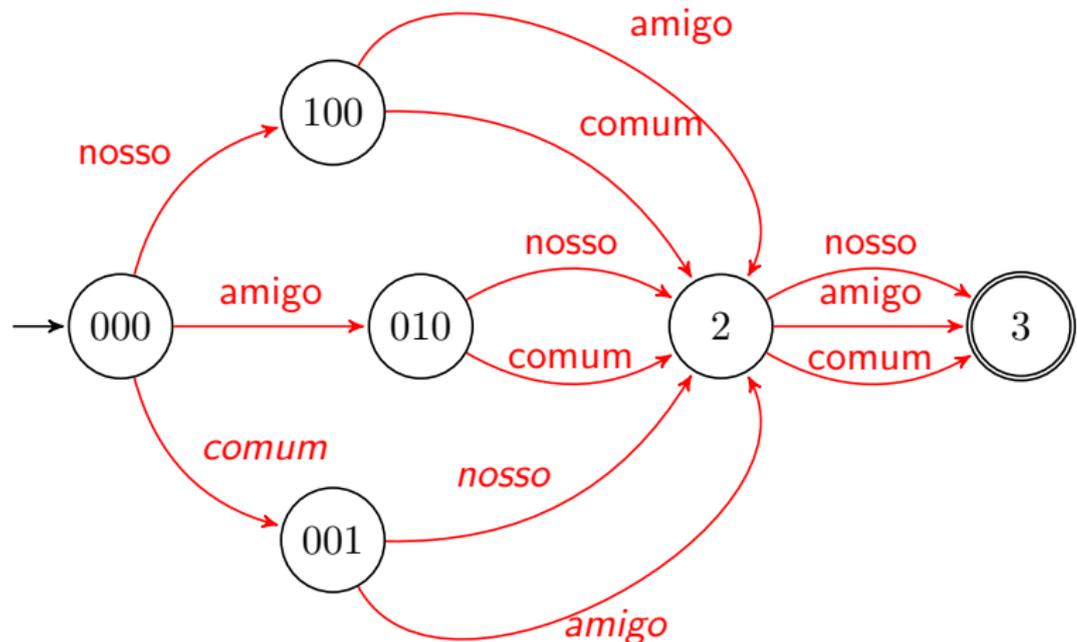
Packing permutations



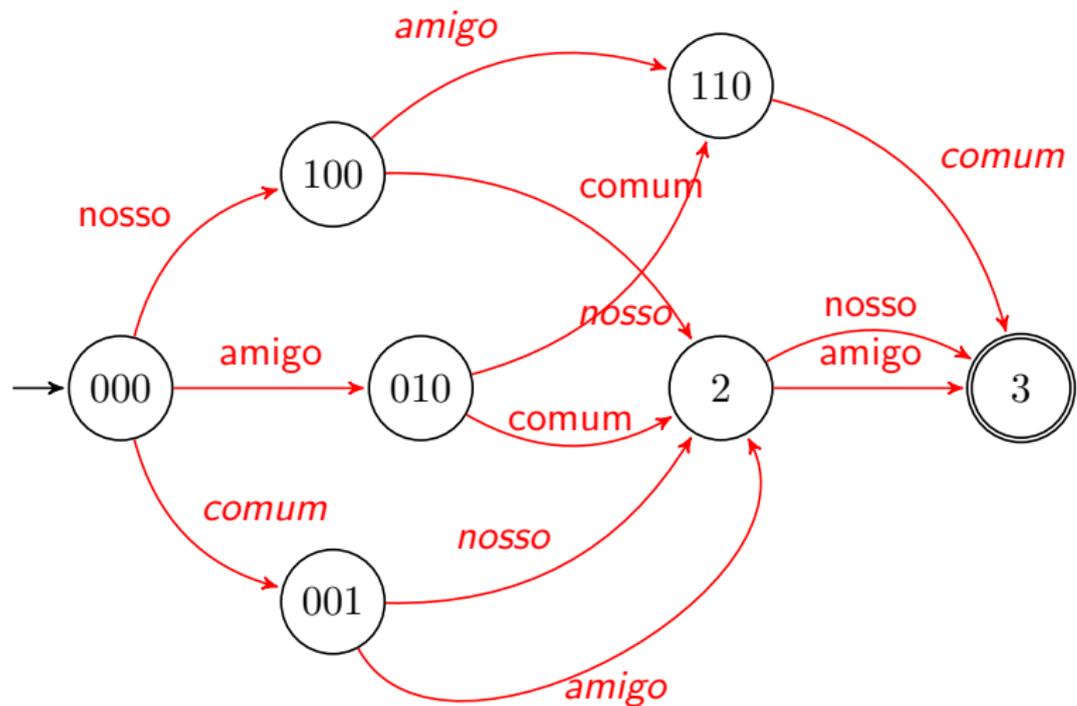
Packing permutations



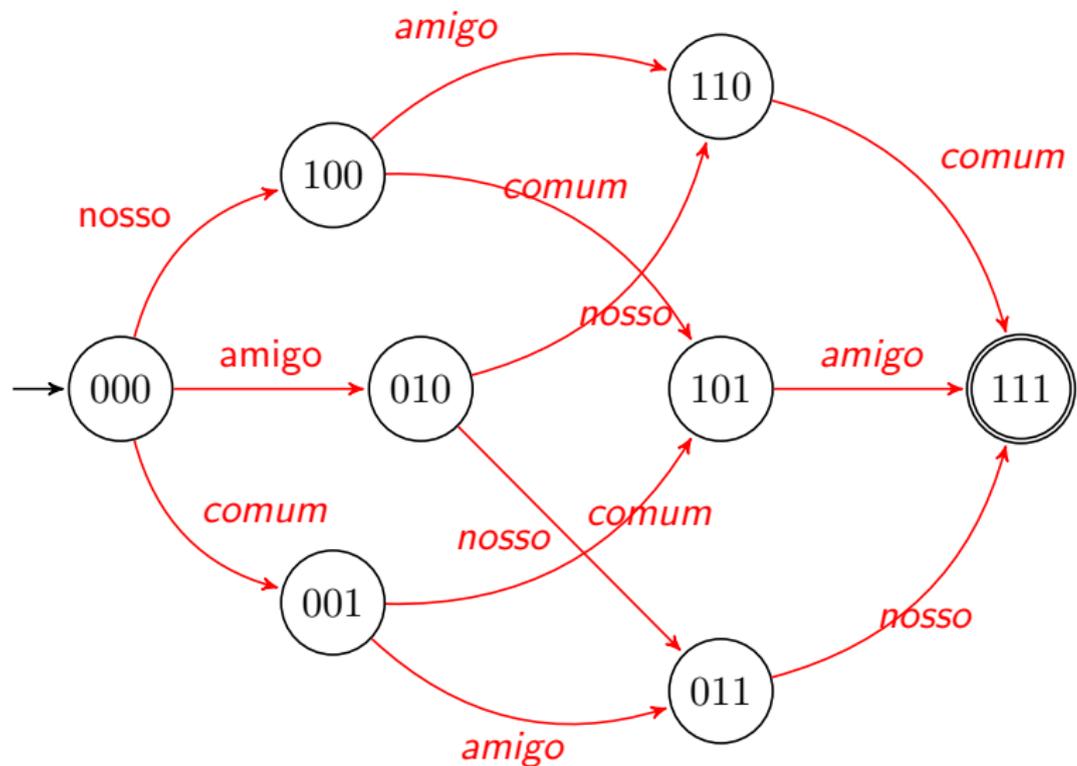
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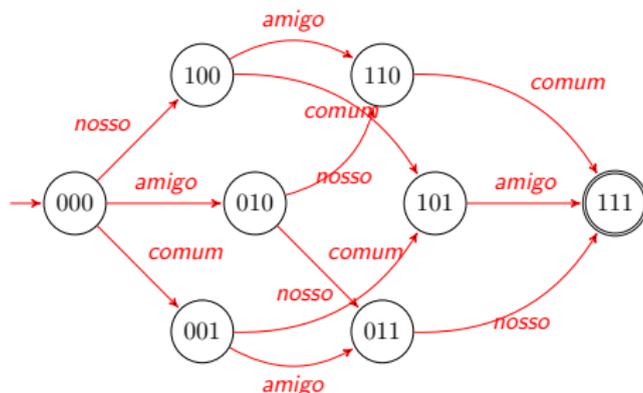
Packing permutations

Powerset (*all subsets*) of $\{1, 2, \dots, I\}$

- ▶ 2^I subsets
think of a vector of I bits ;)

Lattice

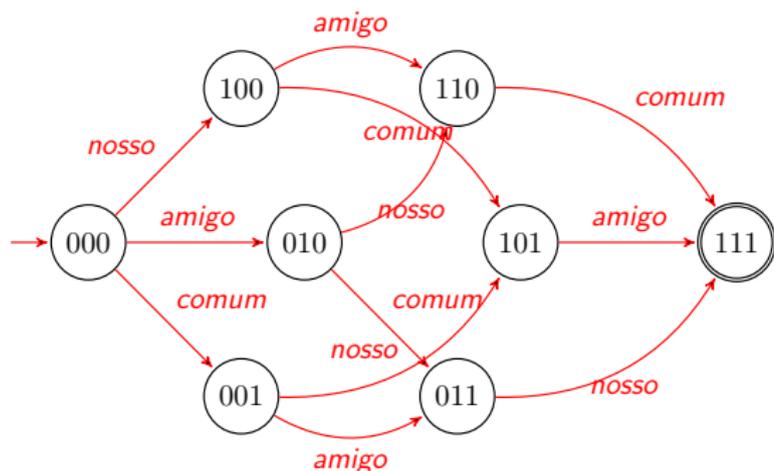
- ▶ $O(2^I)$ states
- ▶ $O(I \times 2^I)$ transitions



Word replacement with unconstrained reordering

Source: *nosso amigo comum*

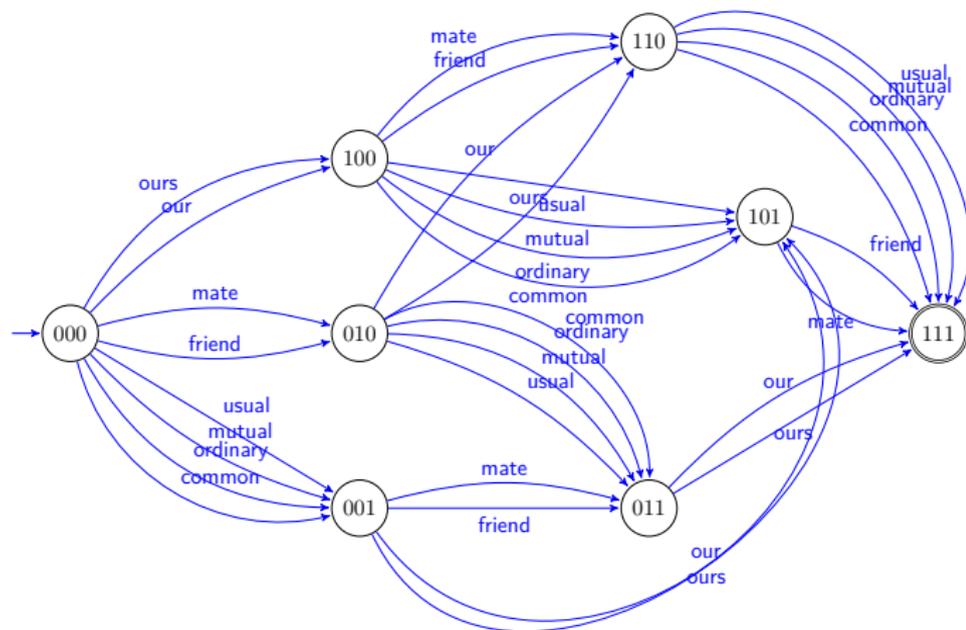
Word replacement with unconstrained reordering



Source: *nosso amigo comum*

1. arbitrary permutations: $O(2^I)$ states

Word replacement with unconstrained reordering



Source: *nosso amigo comum*

1. arbitrary permutations: $O(2^I)$ states
2. intersection with the rule set: $O(tI2^I)$ transitions

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Before we even discuss a parameterisation of the model we already ran into a tractability issue!

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- ▶ **0.o** but how?

Ad-hoc distortion limit

Several flavours of distortion limit [Lopez, 2009]

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Moses allows reordering within a window of length d

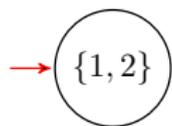
- ▶ starting from the leftmost uncovered word

WL d (example)

Suppose $d = 2$ and $I = 3$

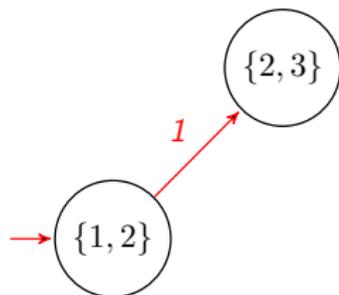
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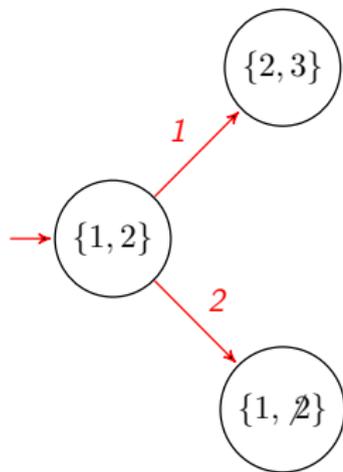
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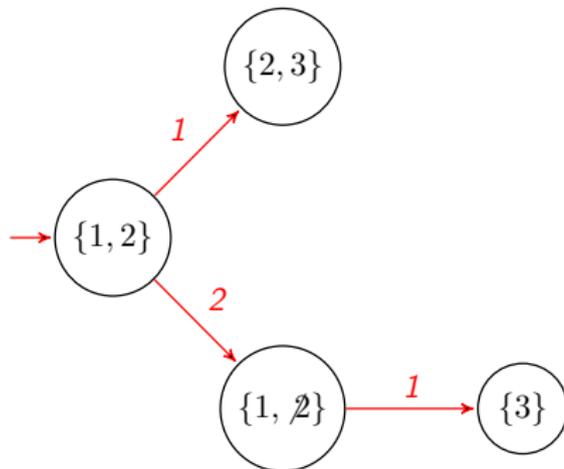
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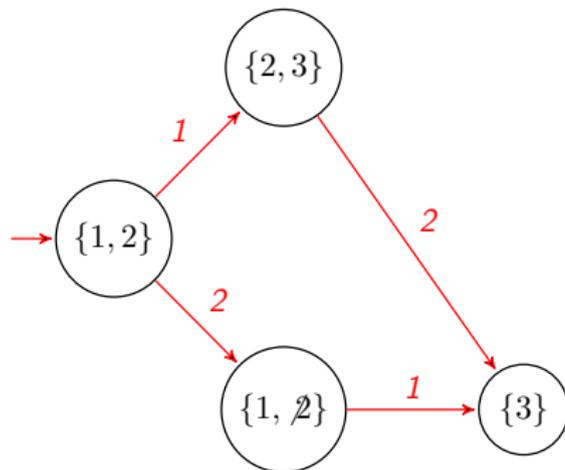
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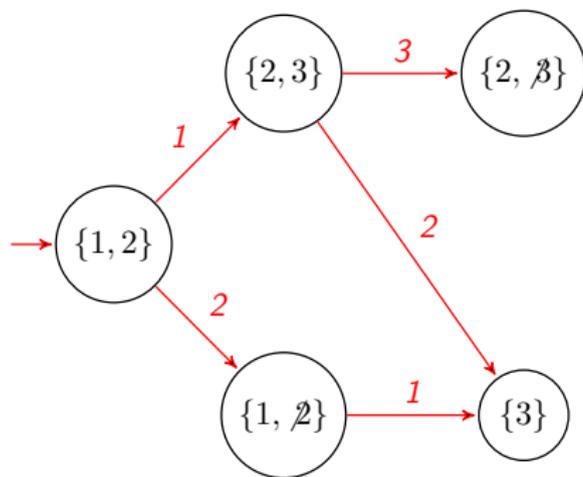
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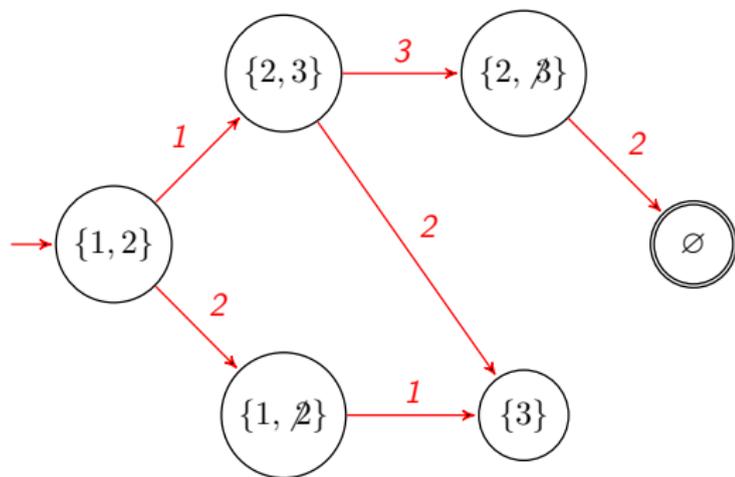
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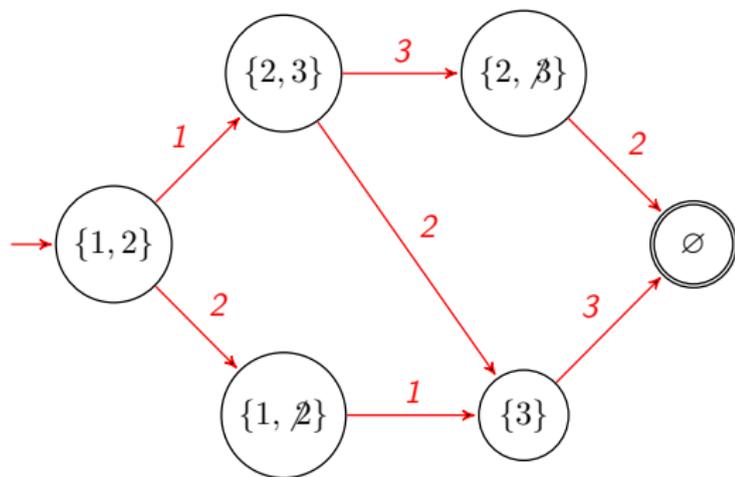
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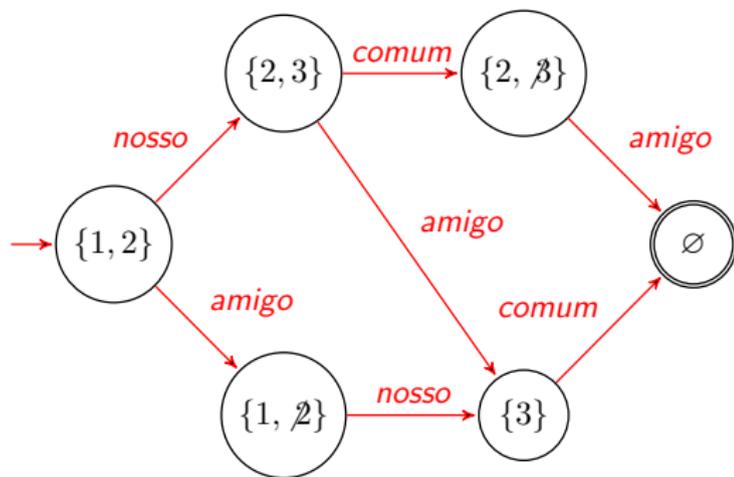
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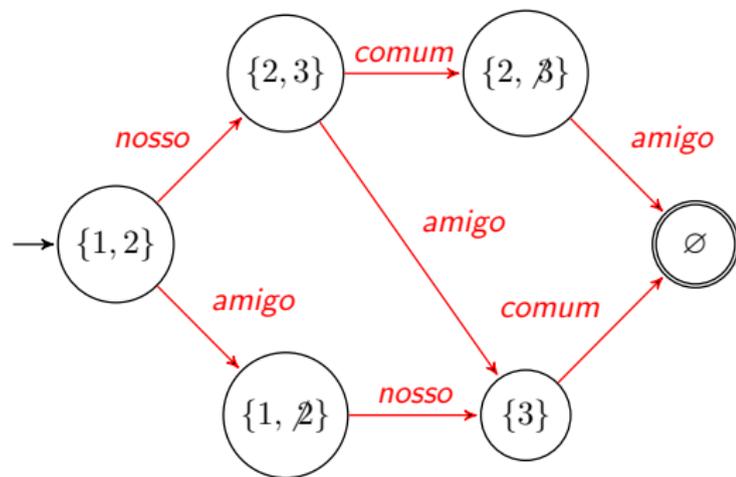
WL d (example)

Suppose $d = 2$ and $I = 3$ (e.g. *nosso amigo comum*)



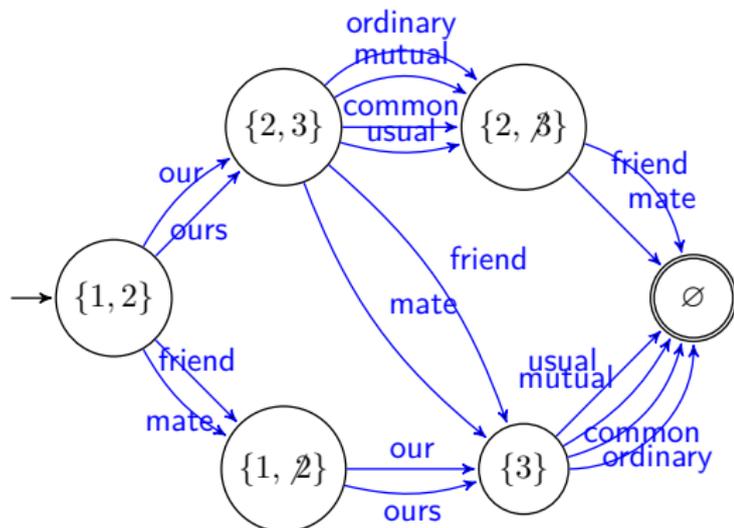
Word replacement with reordering constrained by WL2

Complexity: $O(I2^{d-1})$ states



Word replacement with reordering constrained by WL2

Complexity: $O(tI2^{d-1})$ transitions



Ad-hoc distortion limit: expressiveness

Arbitrarily limit reordering to a fixed-length window

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Ad-hoc distortion limit: expressiveness

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- ▶ what about languages with very different syntax?
e.g. OV vs VO, head-initial vs head-final

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Arbitrarily limit reordering to a fixed-length window

- ▶ convenient (linear complexity), but
- ▶ what about languages with very different syntax?
e.g. OV vs VO, head-initial vs head-final
- ▶ can we do better?

Binary permutations

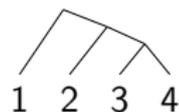
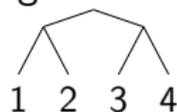
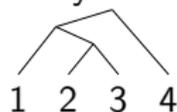
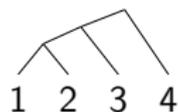
Consider a sentence such that $I = 4$

let's look at binary bracketing trees for this sentence

Binary permutations

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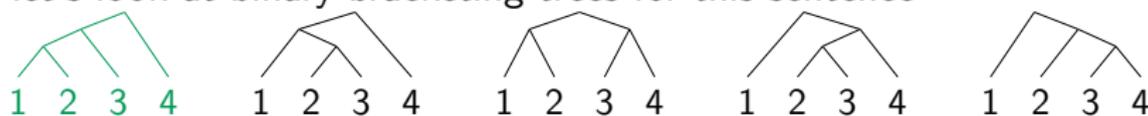
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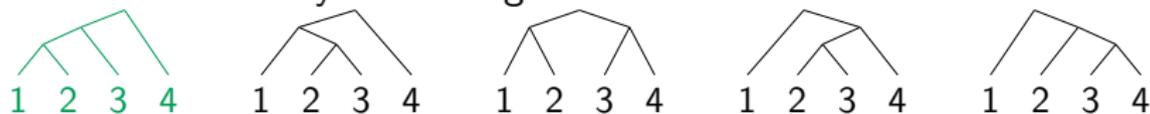
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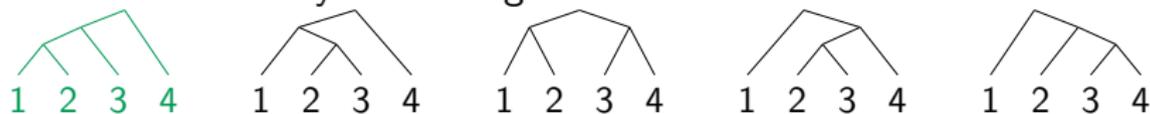
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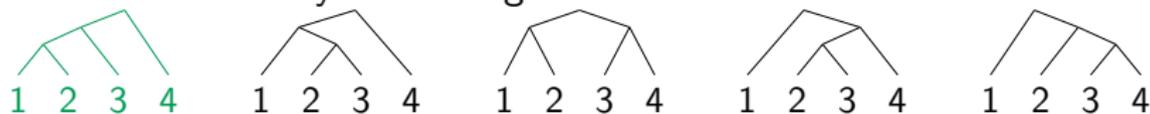
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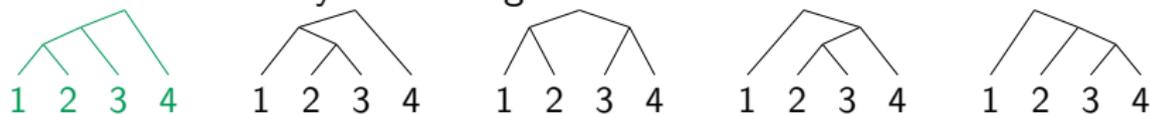
$(\langle\langle 1\ 2 \rangle\rangle)3)4$ 3 1 2 4

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$(\langle\langle 1\ 2 \rangle\rangle)\ 3)\ 4$ 3 1 2 4

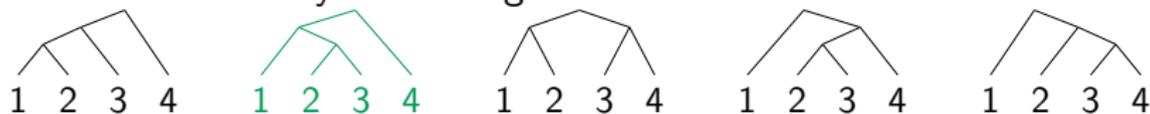
$(\langle\langle\langle 1\ 2 \rangle\rangle\rangle)\ 3)\ 4$ 3 2 1 4

...

Binary permutations

Consider a sentence such that $I = 4$

let's look at binary bracketing trees for this sentence



Binary permutations

$((1(2\ 3))4)$ 1 2 3 4

$((1\langle 2\ 3\rangle)4)$ 1 3 2 4

$(\langle 1(2\ 3)\rangle 4)$ 2 3 1 4

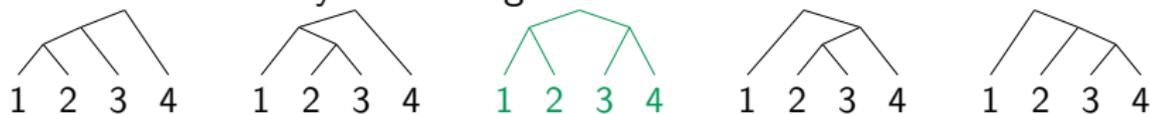
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Binary permutations

$((1\ 2)(3\ 4))$ 1 2 3 4

$(\langle 1\ 2 \rangle (3\ 4))$ 2 1 3 4

$(\langle 1\ 2 \rangle \langle 3\ 4 \rangle)$ 2 1 4 3

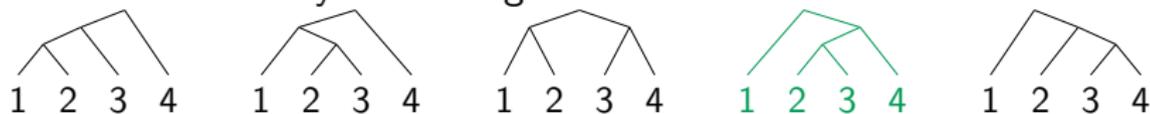
$((1\ 2)\langle 3\ 4 \rangle)$ 1 2 4 3

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Binary permutations

$(1((2\ 3)4))$ 1 2 3 4

$(1(\langle 2\ 3 \rangle 4))$ 1 3 2 4

$(1\langle (2\ 3)4 \rangle)$ 1 4 2 3

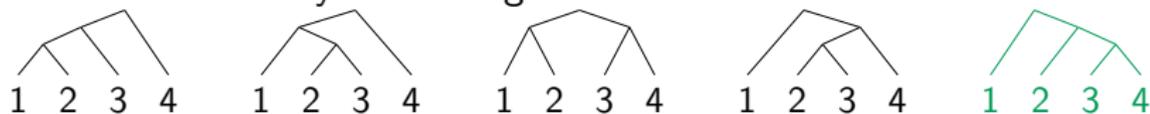
$(1\langle\langle 2\ 3 \rangle\rangle 4)$ 1 4 3 2

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Binary permutations

$(1(2(3 4)))$ 1 2 3 4

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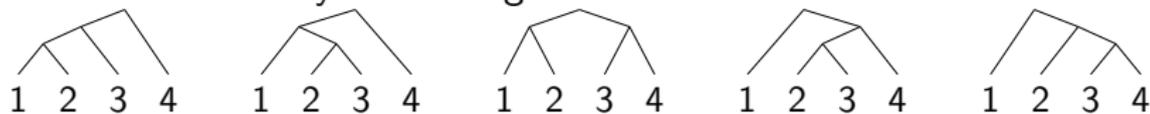
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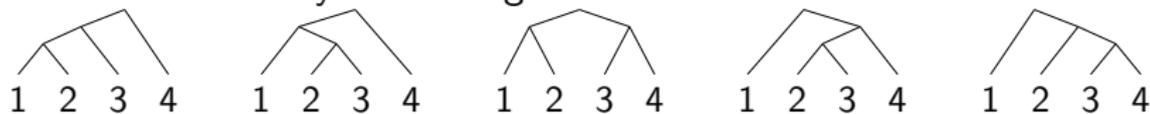
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- ▶ constrains the space of permutations

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Binary permutations

- ▶ constrains the space of permutations
- ▶ crossing constraint

3 1 4 2 ✗

2 4 1 3 ✗

Inversion Transduction Grammars (ITGs) [Wu, 1997]

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- ▶ $X \rightarrow XX$
direct order

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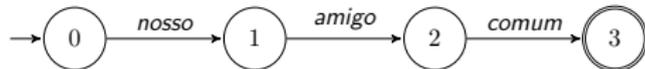
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Inversion Transduction Grammars (ITGs) [Wu, 1997]

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- ▶ $X \rightarrow \langle XX \rangle$
inverted order
- ▶ $X \rightarrow f/e$, where $(f, e) \in R$
bilingual mappings

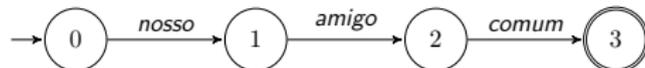
Parsing, intersection and hypergraphs

Source



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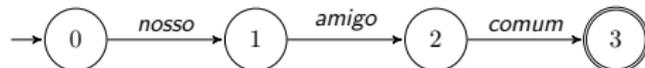


Grammar

$X \rightarrow XX$
 $X \rightarrow \langle XX \rangle$
 $X \rightarrow \textit{nosso}$
 $X \rightarrow \textit{amigo}$
 $X \rightarrow \textit{comum}$

Parsing, intersection and hypergraphs

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Grammar

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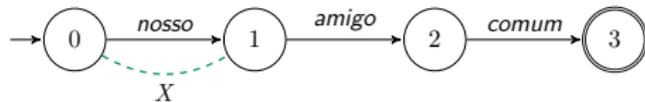
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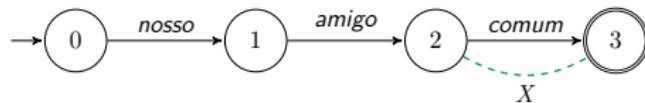
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$X \rightarrow XX$
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Parsing, intersection and hypergraphs

Source



Grammar

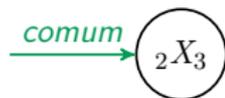
$X \rightarrow XX$

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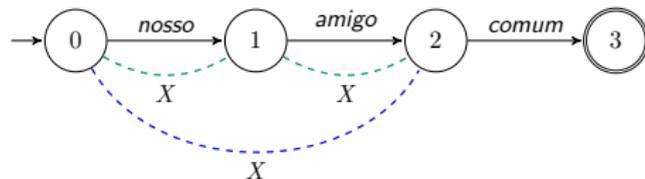
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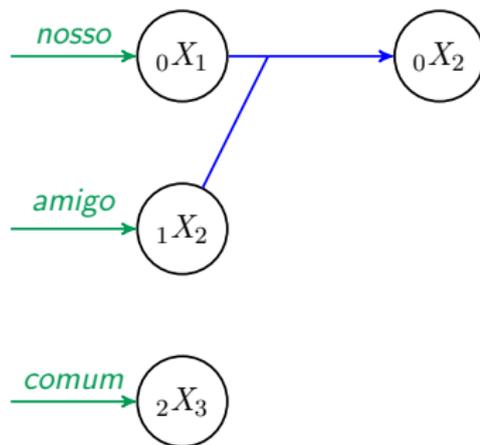
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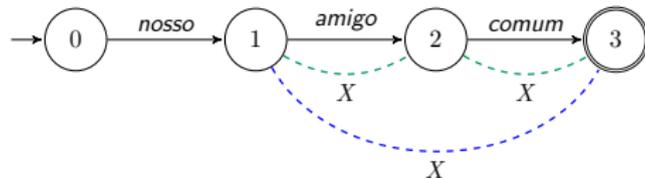
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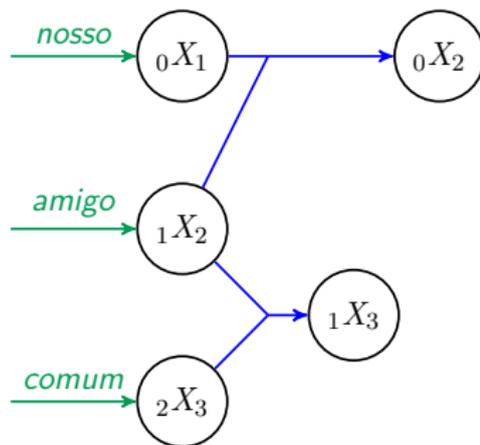
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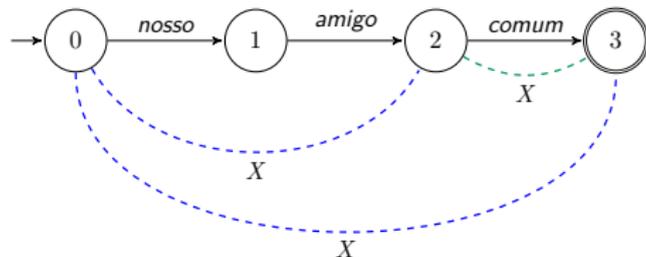
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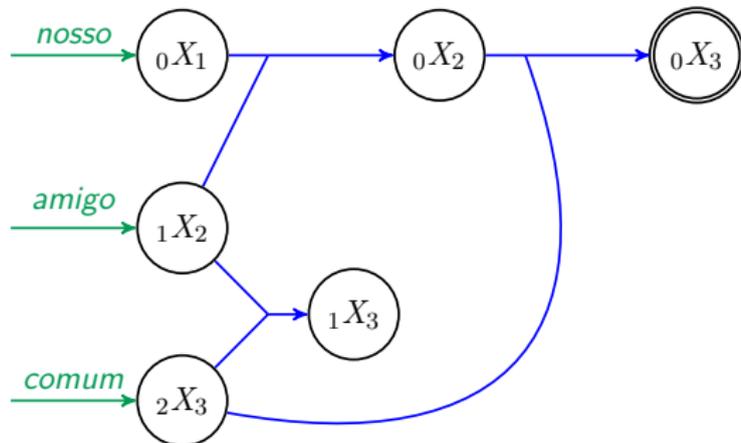
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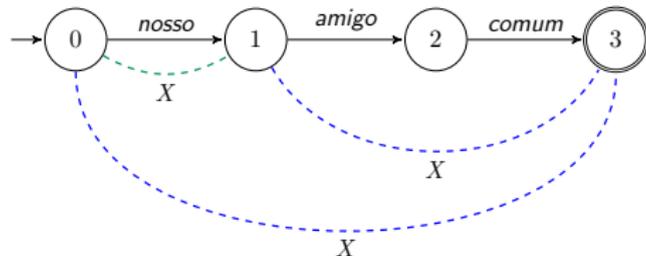
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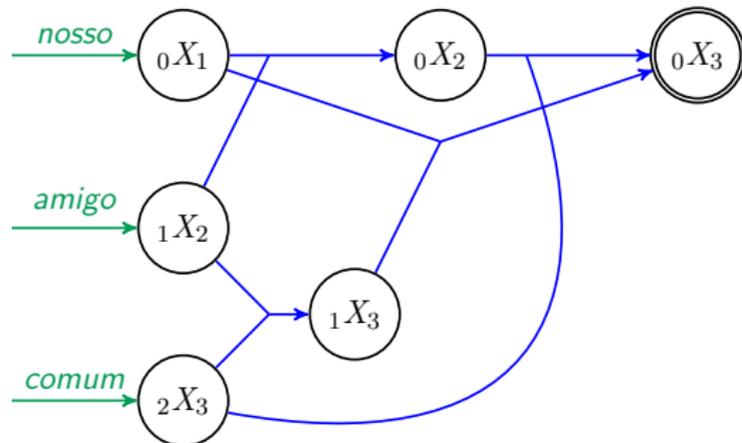
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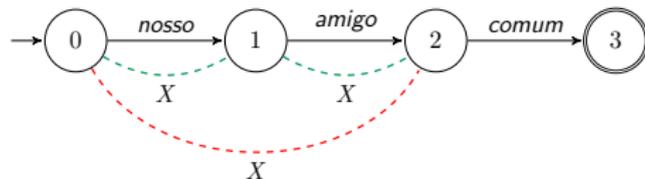
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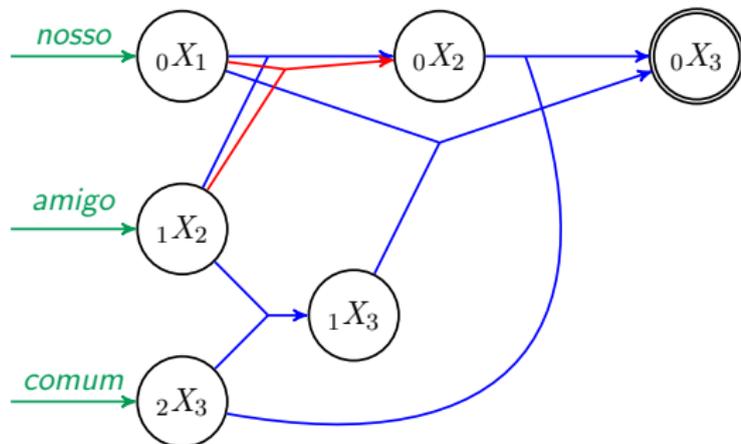
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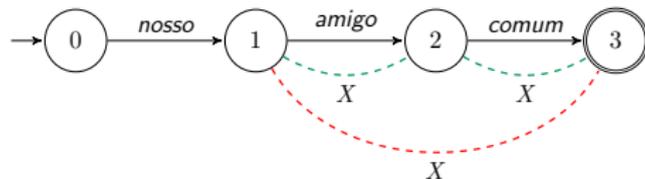
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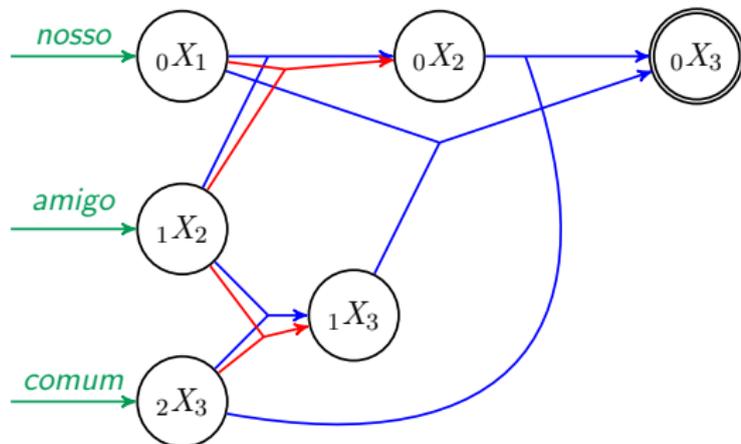
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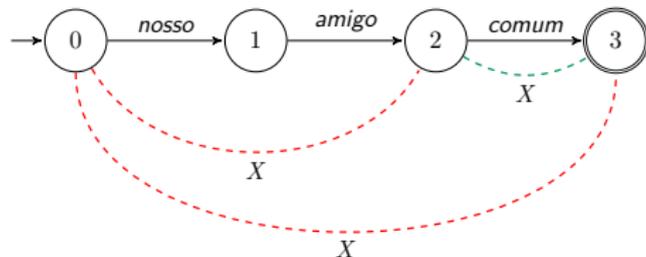
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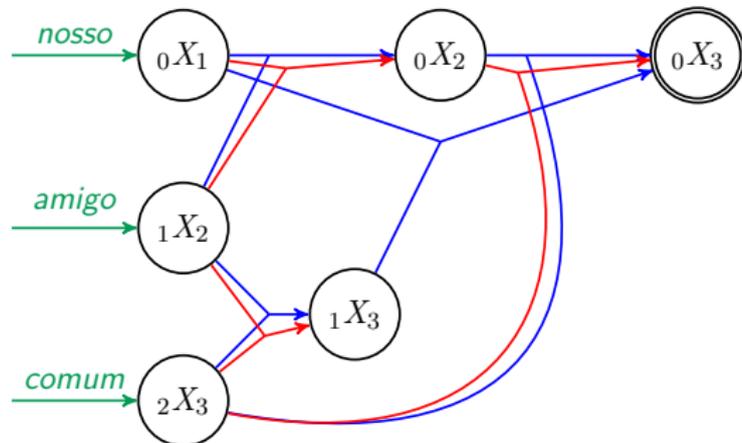
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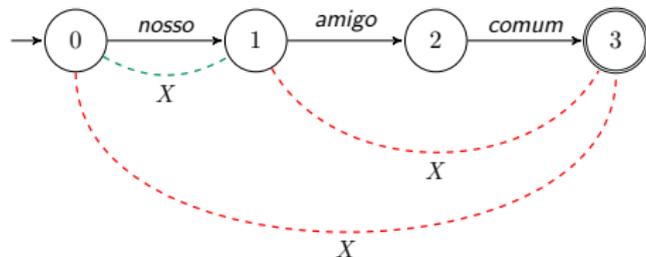
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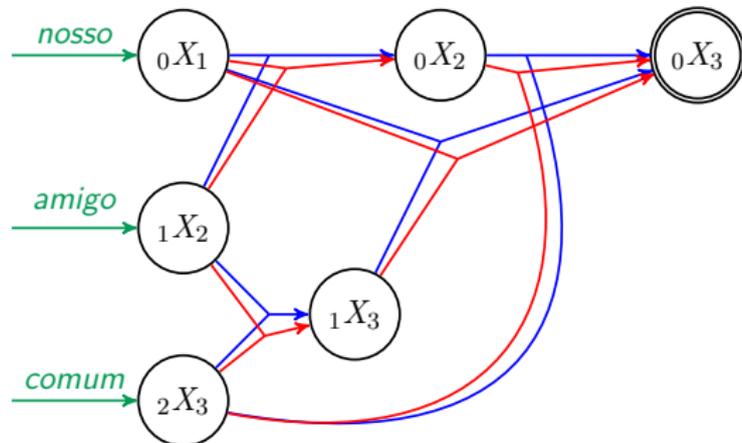
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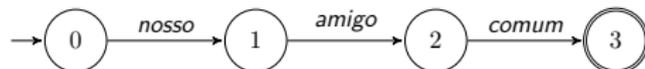
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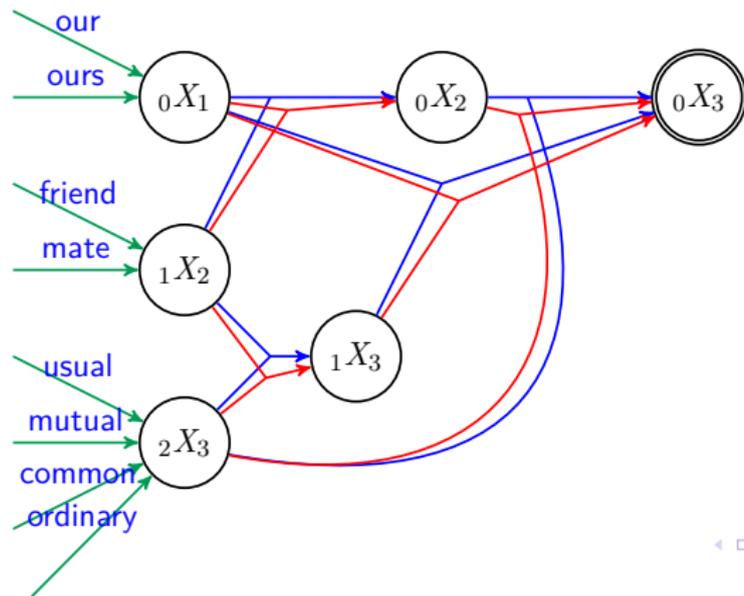
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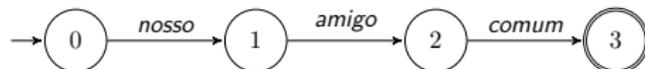
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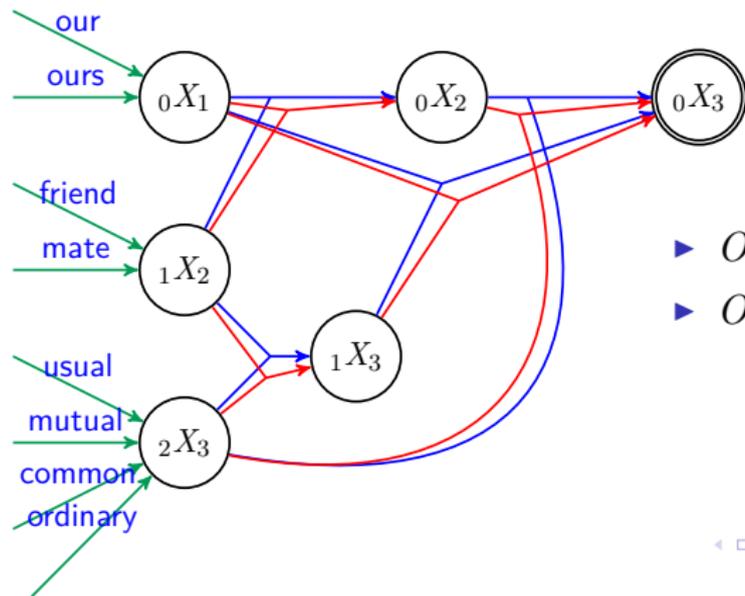
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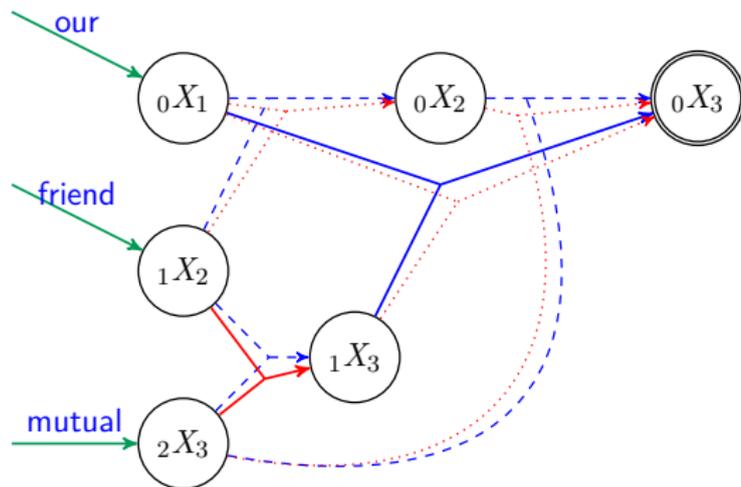
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- ▶ $O(I^3)$ nodes
- ▶ $O(tI^3)$ edges

Example

(nosso **amigo comum**) → **our mutual friend**



Recap 2

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But we still perform translation word-by-word with no insertion or deletion!

1-1 mappings: fail!

Source: o₁ grilo₂ *da*₃ lareira₄

Target: the₁ cricket₂ [on the]₃ hearth₄

Insertion and deletion

Implicitly modelled by moving from words to phrases

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Mappings of contiguous sequences of words

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e.g. *a loja de antiguidades*/old curiosity shop

Generalising the rule set (FST)

Rules

<i>o</i>	{the, a}
<i>grilo</i>	{cricket, annoyance}
<i>da</i>	{on the, of, from}
<i>hearth</i>	{lareira}

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Using FST

- ▶ each rule can be seen as a transducer

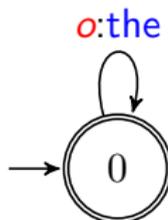
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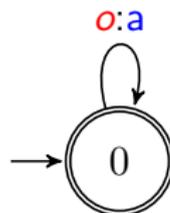
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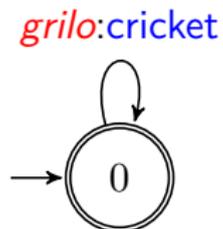
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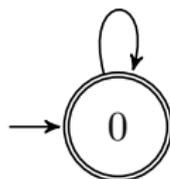
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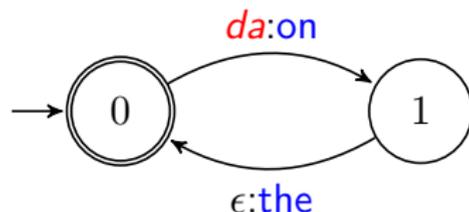
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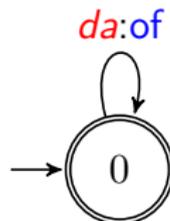
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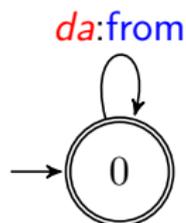
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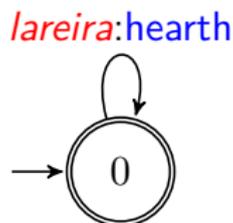
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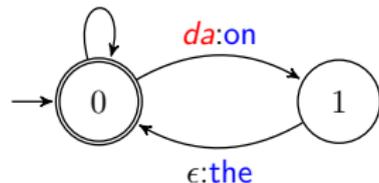
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Using FST

- ▶ each rule can be seen as a transducer
- ▶ the union represents the rule set
- ▶ standard intersection mechanisms do the rest

Phrase permutations' translation with WL_d

We can translate a lattice encoding the WL_d permutations

Phrase permutations' translation with WL^d

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- ▶ a truncated window controls reordering
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 - ▶ $O(I^2)$ segments
 - ▶ it is sensible to limit phrases to a maximum length
- ▶ complexity remains
 - ▶ linear with sentence length
 - ▶ exponential with distortion limit

Generalising the rule set (ITG)

Simply extend the terminal rules

Generalising the rule set (ITG)

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- ▶ $X \rightarrow XX$
direct order

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The intersection mechanisms do the rest

- ▶ $O(I^3)$ nodes (phrases are limited in length)
- ▶ $O(tI^3)$ edges

Recap 3

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2. efficiently represented the set of translations supported by these models for a given input sentence
 - ▶ trivially expressed in terms of intersection/composition
 - ▶ a logic program can do the same
(sometimes more convenient, e.g. WLD constraints)

Remarks

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- ▶ the space of solutions is cubic in length
- ▶ however less efficiently packed, better motivated constraints on reordering

Remarks (hiero)

Hierarchical phrase-based models [Chiang, 2005]

¹Other than monotone translation with *glue rules* 

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We have characterised the set of solutions “backed” by our transfer model

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We are missing a parameterisation of the model

- ▶ the scoring function which will guide the decision making process

Linear models

Let's call **derivation**

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Think of it as a surrogate for translation quality at decoding time

[Berger et al., 1996]

[Och and Ney, 2002]

Feature functions

Independently capture different aspects of the translation, such as

- ▶ adequacy
 - ▶ translation probabilities
 - ▶ confidence on lexical choices
- ▶ fluency
 - ▶ LM probabilities
 - ▶ confidence on reordering

Independence assumptions

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Structural independence: scoring rules in isolation

Scoring rules independently



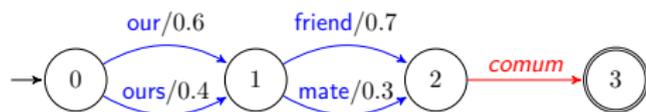
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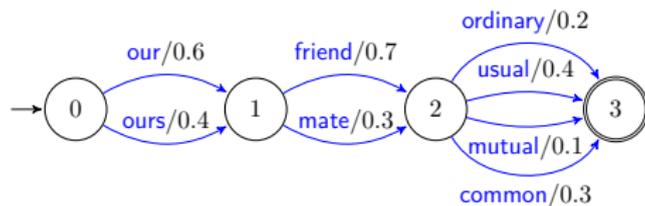
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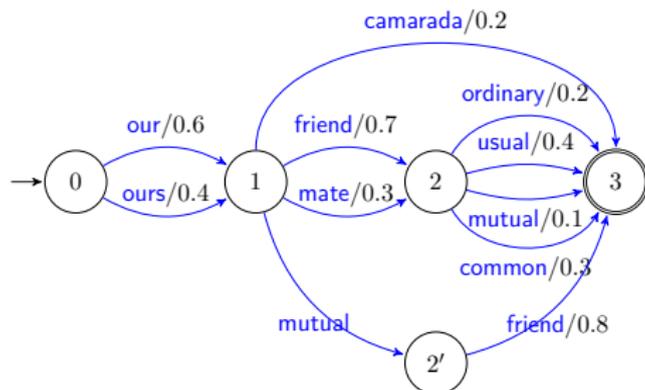
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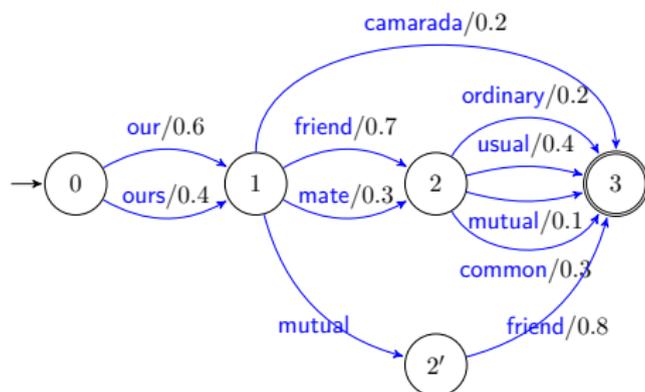
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inference runs in time linear with the size of the automaton

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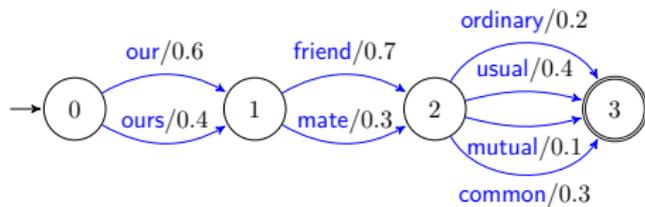
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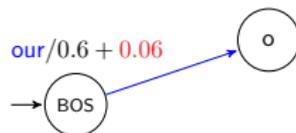
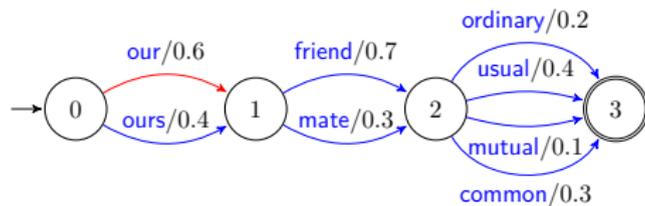
- ▶ fluency as captured by an n -gram LM component

Scoring strings with a 2-gram LM



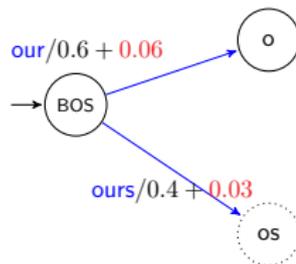
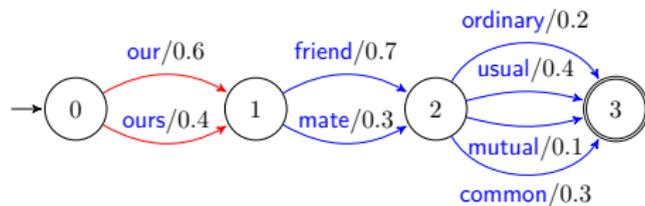
requires unpacking the representation

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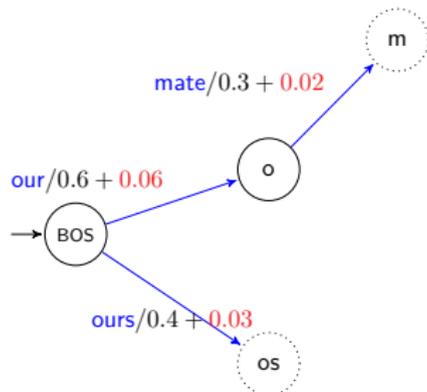
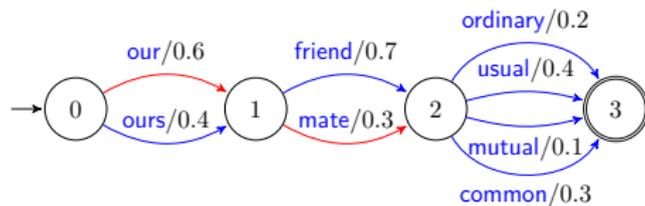
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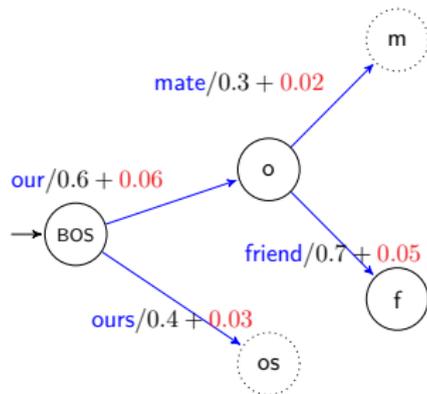
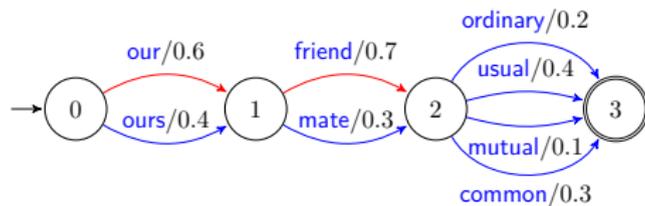
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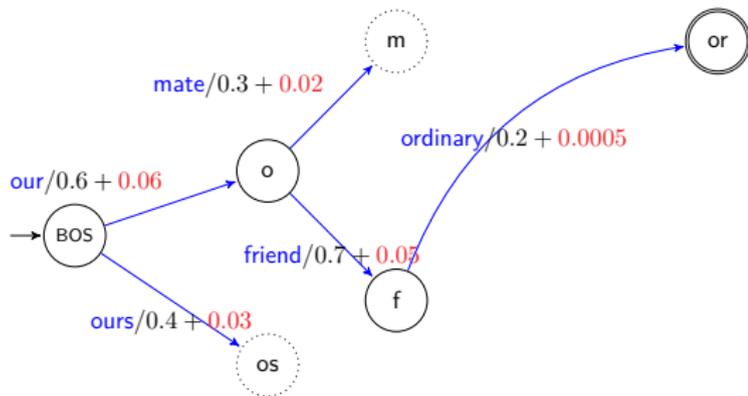
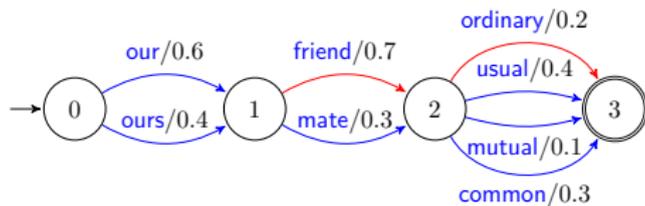
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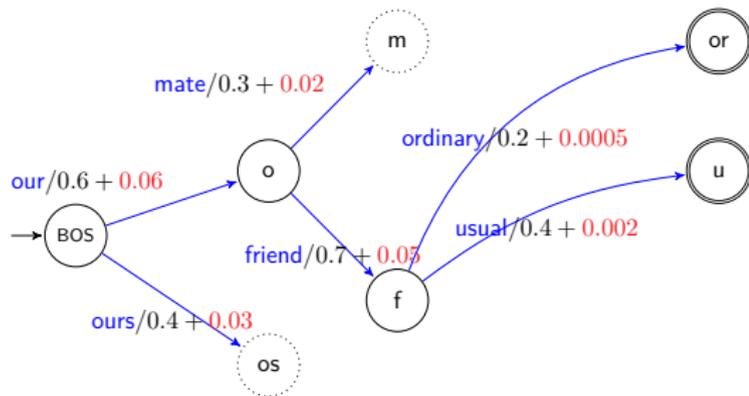
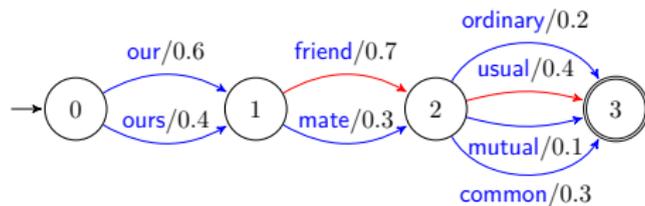
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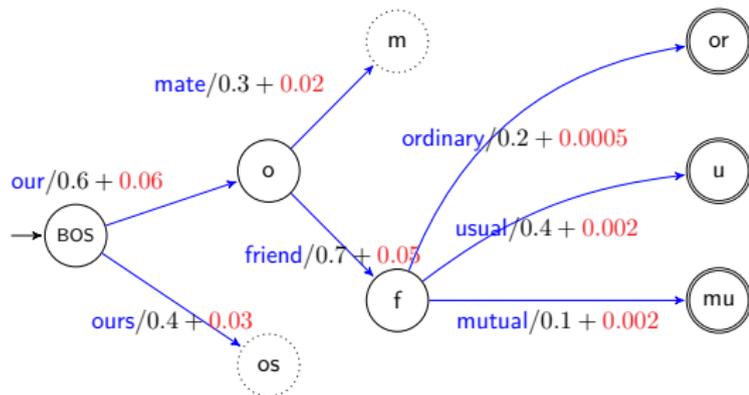
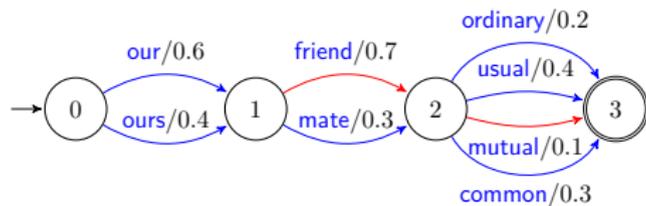
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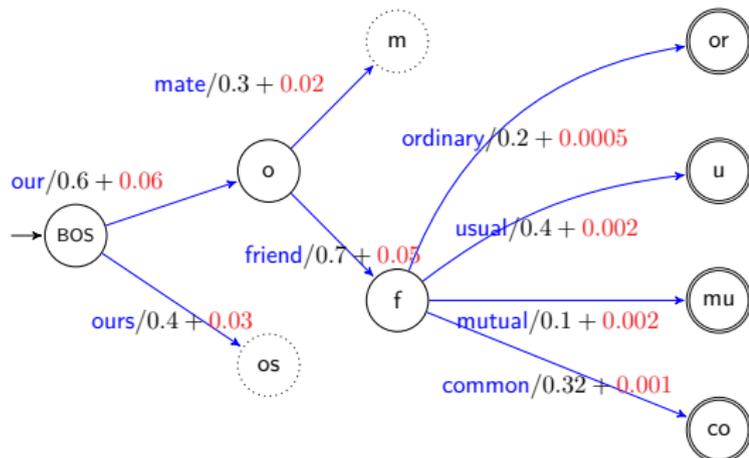
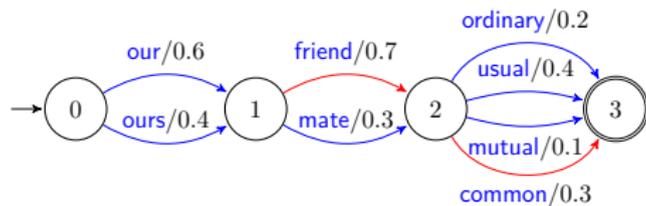
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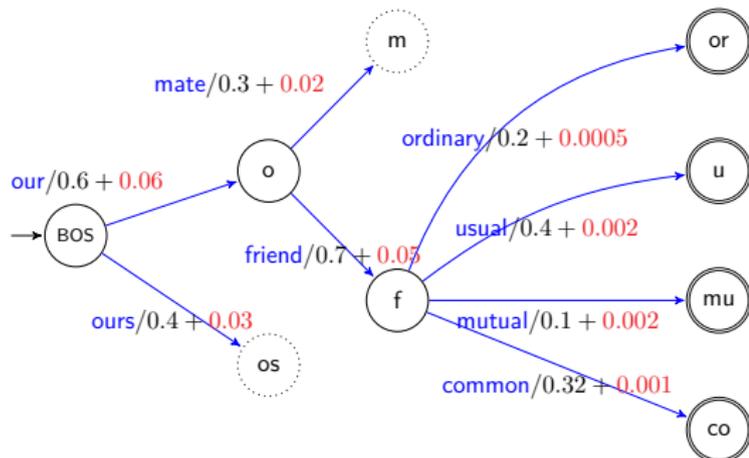
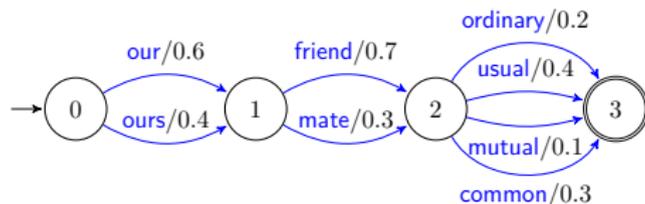
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e.g. via suffix arrays [Zhang and Vogel, 2006]
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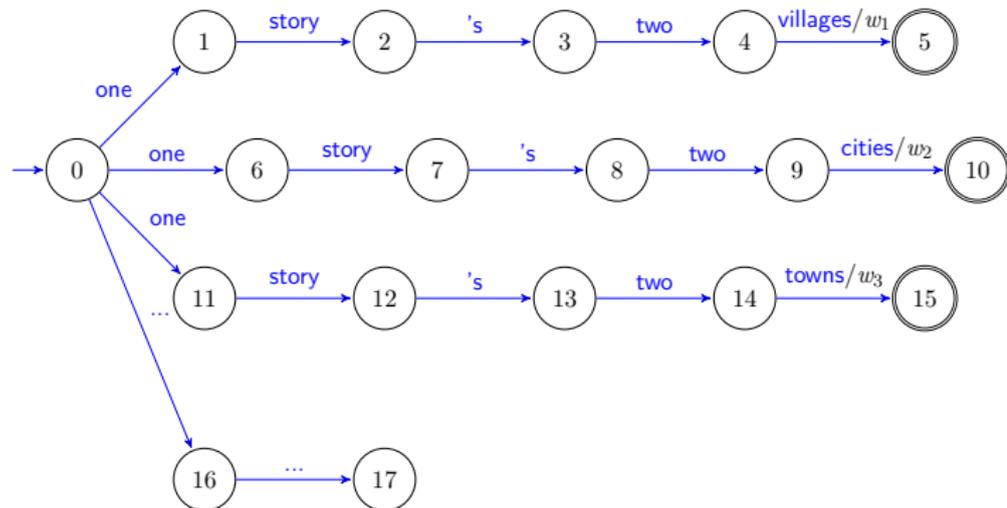
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- ▶ requires fully unpacking the representation
- ▶ making dependencies explicit through the graphical structure

Scoring whole sentences: example



Exhaustive enumeration

- ▶ number of edges exponential with input length
- ▶ **intractable**

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- ▶ nodes must group derivations sharing the same context
- ▶ polynomial, though often prohibitive (**impracticable**)

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- ▶ more examples of models and impact on representation
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 - ▶ a global feature function
- ▶ inference algorithms
- ▶ techniques to make inference feasible for interesting models

Picking one solution

What do we pick out of the (whole) weighted space of solutions?

- ▶ best translation
- ▶ “minimum-loss” translation

Best translation

MAP

$$\mathbf{y}^* = \operatorname{argmax}_{\mathbf{y}} \sum_{\mathbf{d}[\mathbf{d}=\mathbf{y}]} f(\mathbf{d}|\mathbf{x})$$

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NP-complete: related to determinisation [Sima'an, 1996]

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Viterbi (approximation to MAP)

$$\mathbf{d}^* = \operatorname{argmax}_{\mathbf{d}} f(\mathbf{d}|\mathbf{x})$$

- ▶ assumes the most likely derivation is enough

Minimum Bayes Risk translation

MBR

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- ▶ incorporates a loss (or gain) function

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$$\mathbf{y} = \underset{\mathbf{y}}{\operatorname{argmin}} \langle \operatorname{loss}(\mathbf{y}, \mathbf{y}') \rangle_{p(\mathbf{y}'|\mathbf{x})}$$

Minimum Bayes Risk translation

MBR

- ▶ incorporates a loss (or gain) function

$$\mathbf{y} = \operatorname{argmax}_{\mathbf{y}} \langle \text{gain}(\mathbf{y}, \mathbf{y}') \rangle_{p(\mathbf{y}'|\mathbf{x})}$$

Minimum Bayes Risk translation

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- ▶ incorporates a loss (or gain) function

$$\mathbf{y} = \operatorname{argmax}_{\mathbf{y}} \langle \text{BLEU}(\mathbf{y}, \mathbf{y}') \rangle_{p(\mathbf{y}'|\mathbf{x})}$$

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- ▶ incorporates a loss (or gain) function

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- ▶ assesses the risk associated with choosing any one translation

Minimum Bayes Risk translation

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- ▶ which requires a **probability**

$$p(\mathbf{d}|\mathbf{x}) = \frac{f(\mathbf{d}|\mathbf{x})}{\sum_{\mathbf{d}'} f(\mathbf{d}'|\mathbf{x})}$$

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- ▶ can be estimated from samples of derivations
- ▶ have a look at project 14 ;)

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- ▶ heuristic view of outside weights

DP-based Viterbi

Explore a truncated version of the full space

- ▶ only a budgeted set of outgoing edges from each node
 - ▶ beam search: exhaustively enumerates outgoing edges, ranks them, prunes all but k -best
 - ▶ cube pruning: enumerates k edges in near best-first order

In order to compare hypotheses more fairly

- ▶ future cost estimates
- ▶ heuristic view of outside weights
- ▶ cheap dynamic program that estimates the best possible way to complete any translation prefix

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[Koehn et al., 2003]

[Chiang, 2007]

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[Kumar and Byrne, 2004]

[Tromble et al., 2008]

Sampling

Gibbs sampling

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Importance sampling

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Importance sampling

- ▶ you will hear from us (project 14) ;)

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Advantages

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2. potential to incorporate arbitrarily complex features (at the sentence level at least)
3. sometimes unbiased
4. ideal for MBR and tuning
5. typically stupid simple to parallelise

Thanks!

Questions?

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